

NPL's progress towards absorbed dose standards for proton beams

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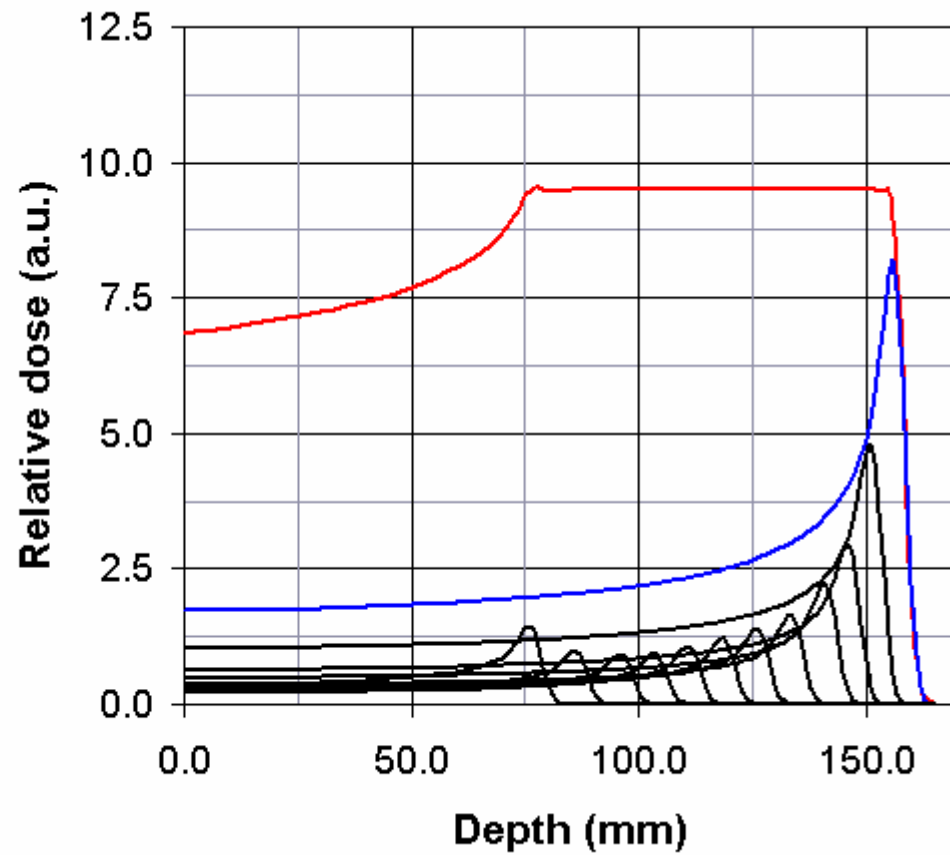
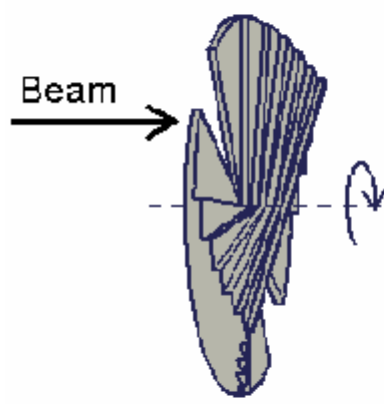
- Proton therapy and to a lesser extent ion therapy are treatment modalities of increasing importance
- Dosimetry has not been as well established as in high-energy x-ray beams
- NPL's activities in improving proton and ion dosimetry:
 - SR project 2002-2004
 - Graphite calorimetry
 - Interaction data
 - Alanine dosimetry
 - Monte Carlo simulation of perturbation correction factors

Topics discussed in this talk



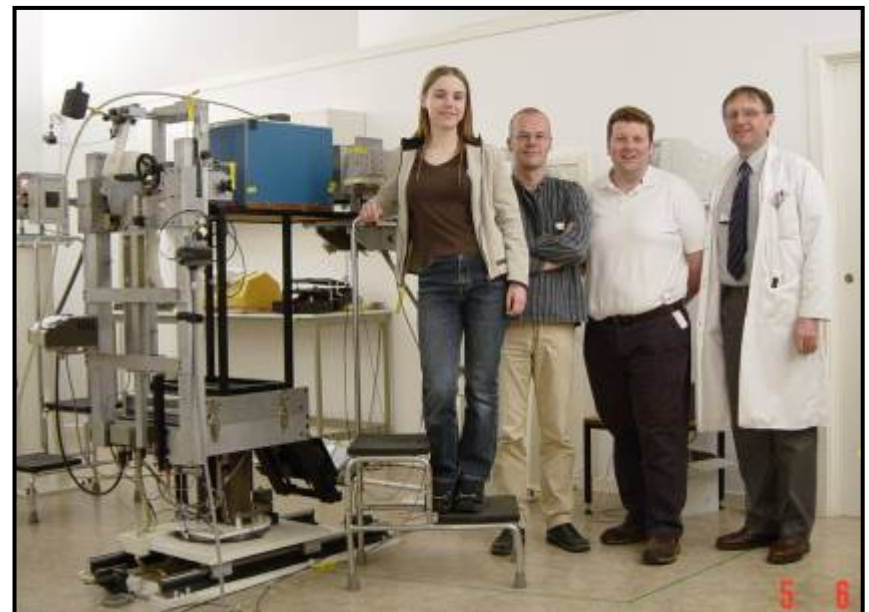
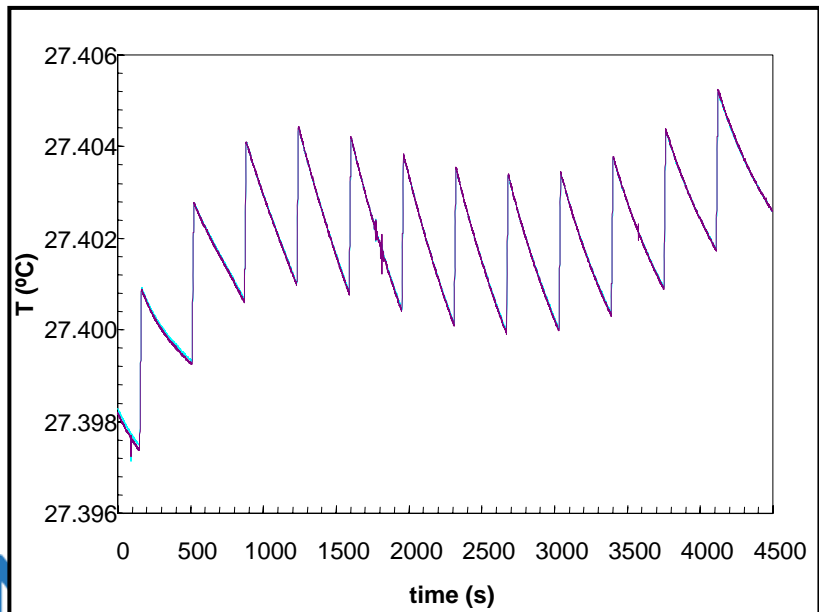
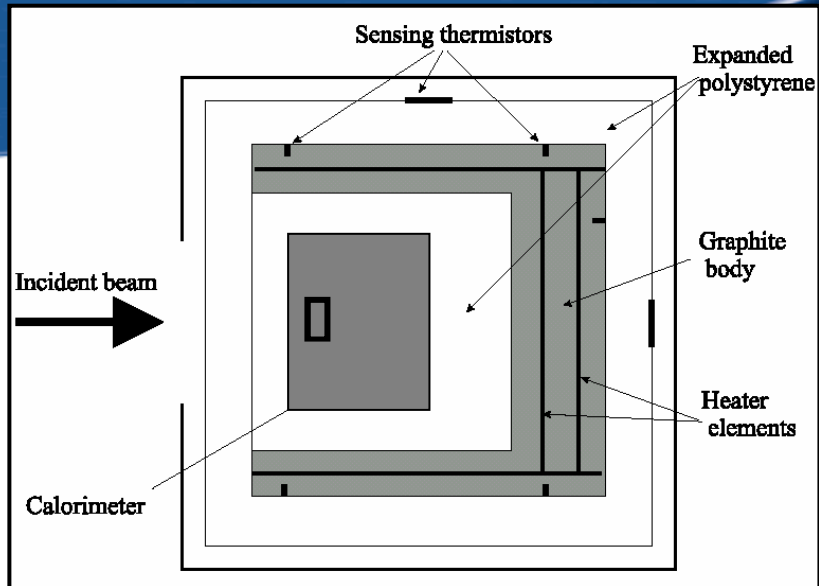
- Calorimetry
 - Graphite calorimetry in CCO beam
 - Development of a primary standard level graphite calorimeter for light-ions
- Interaction/basic data
 - $(w_{\text{air}})_p$ value
 - Stopping powers
 - Non-elastic nuclear interaction cross sections
- Correction factors for ionization chambers related to:
 - Recombination
 - Dose gradients
 - Secondary electrons
 - Non-elastic nuclear interactions

Why protons?



Graphite calorimetry for protons CCO

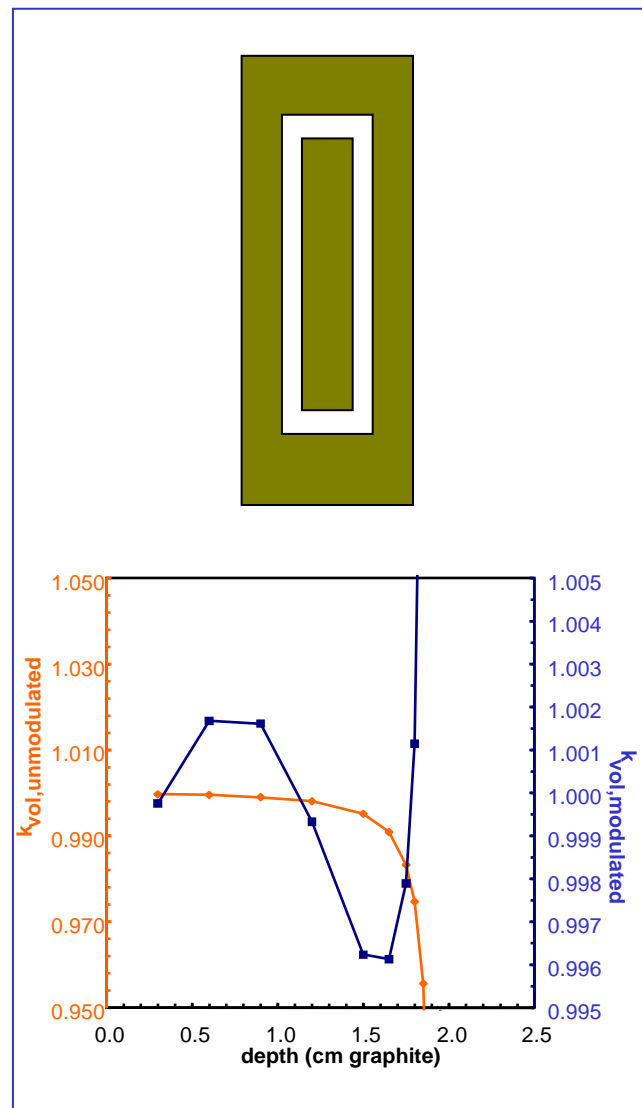
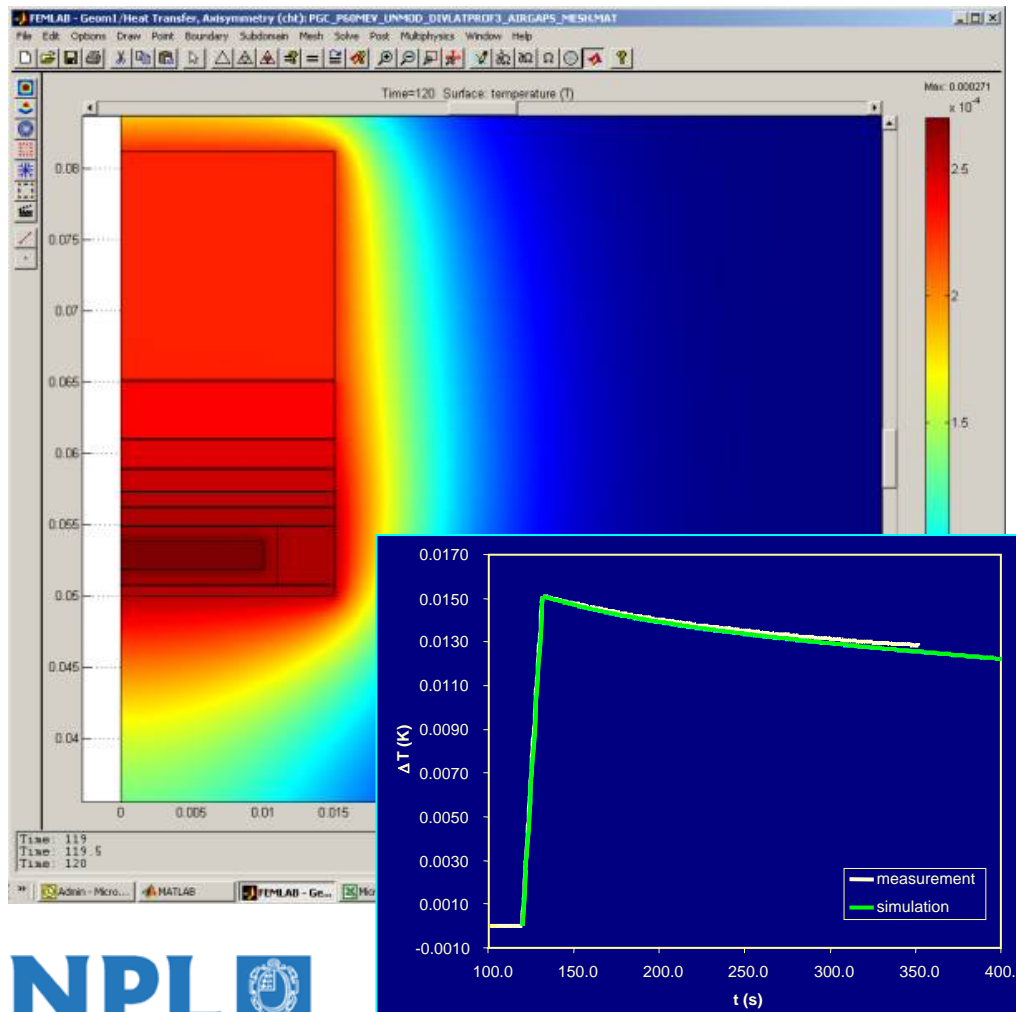
(Palmans et al 2004, Phys Med Biol 49:3737-49)



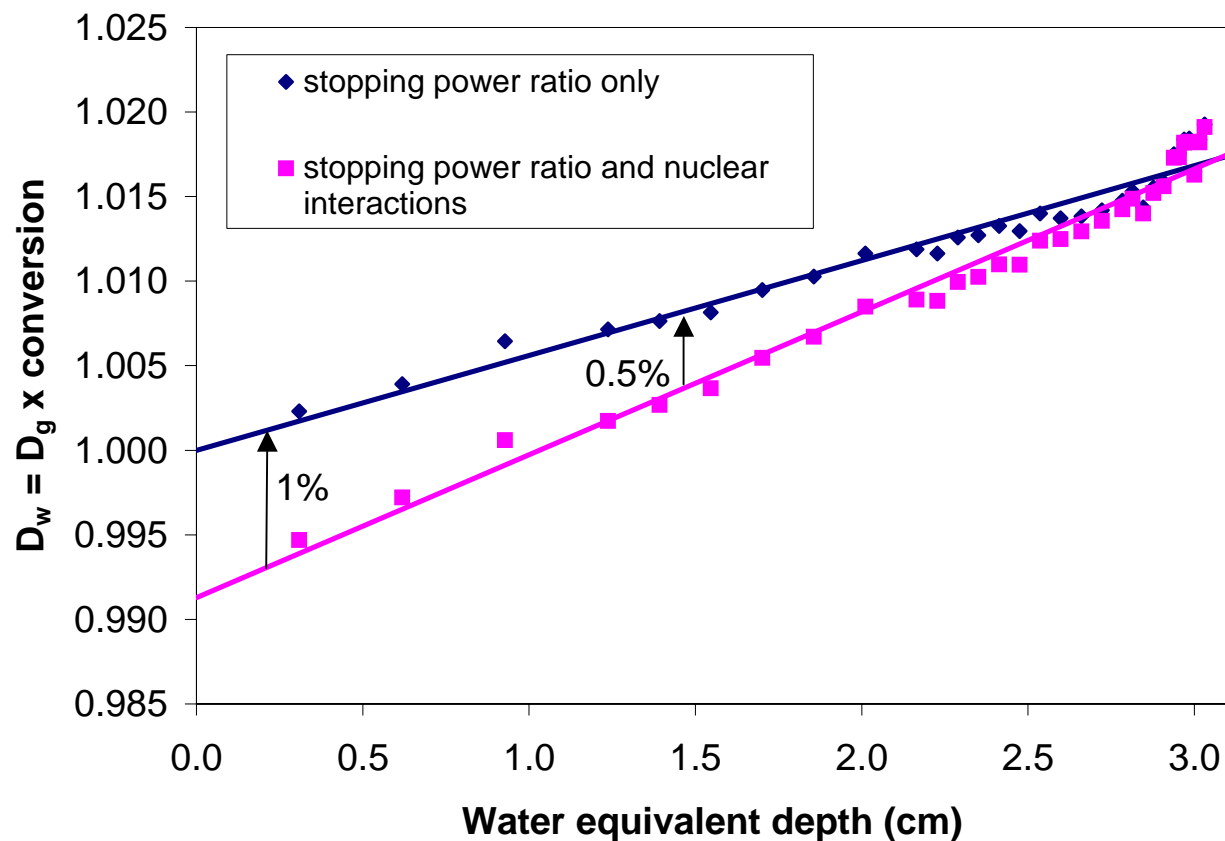
Graphite calorimetry for protons CCO (Palmans et al 2004, Phys Med Biol 49:3737-49)

Volume/gap effects:
MC (McPTRAN.RZ)

Heat transfer: FE (Comsol)



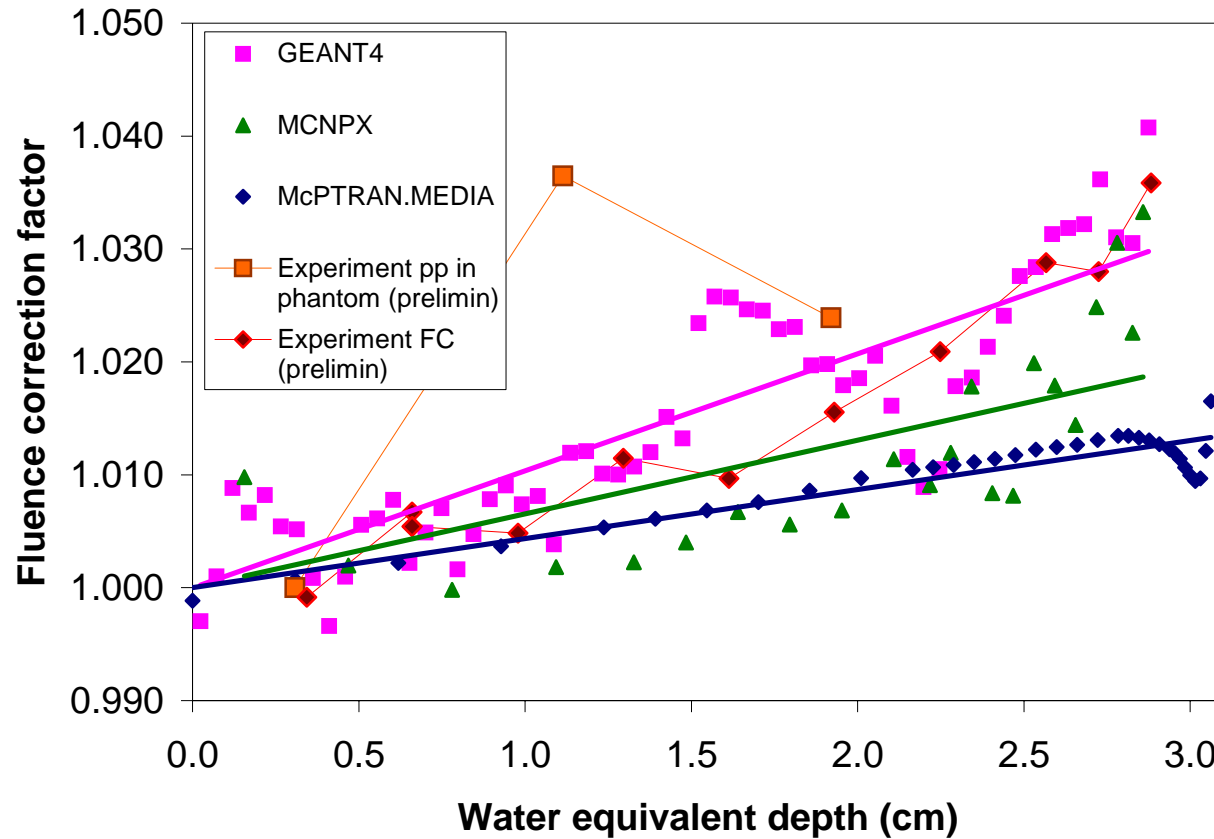
Graphite to water conversion 2: dose conversion (ICRU-49 and ICRU-63)



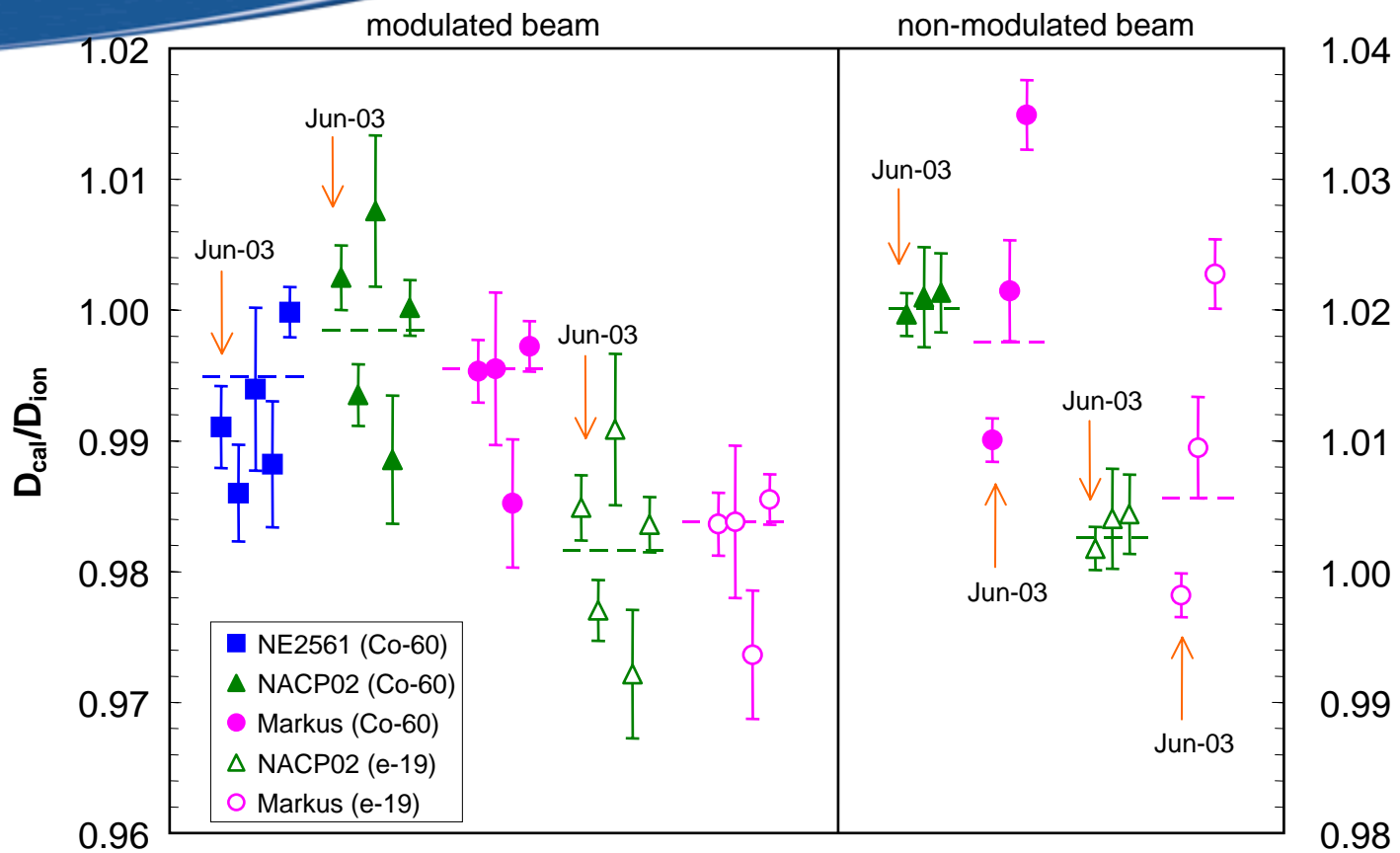
$$D_w(z_w) = D_g(z_g) \cdot s_{w,g}$$

$$D_w(z_w) = D_{g,C}(z_g) \cdot s_{w,g} + D_{g,N}(z_g) \cdot (\sigma_n/A)_{w,g}$$

Graphite to water conversion 3: fluence correction



Graphite calorimetry results CCO



| Calibration beam quality | $D_{w,SPGC}/D_{w,IC}$ | |
|--------------------------|-----------------------|---------------|
| | modulated | non-modulated |
| ^{60}Co | 0.996 | 1.019 |
| e_{e19} | 0.983 | 1.004 |

Uncertainty

| Source of uncertainty | Based on ^{60}Co | Based on Q_{e19} | type |
|--|---------------------------|--------------------|------|
| | <i>for SPGC</i> | | |
| <u>thermistor calibration</u> | | 0.10 | B |
| <u>specific heat</u> | | 0.08 | B |
| <u>$s_{w,g}$</u> | | 1.00 | B |
| <u>k_{gan}</u> | | 0.05 | A |
| <u>k_{volume}</u> | | 0.05 | A |
| <u>extrapolation</u> | | 0.06 | B |
| | <i>for NACP-02</i> | | |
| <u>reproducibility</u> | 0.29 | 0.27 | A |
| <u>positioning</u> | 0.30 | 0.30 | B |
| <u>P_{ion}</u> | 0.10 | 0.10 | B |
| <u>P_{pT}</u> | 0.05 | 0.05 | B |
| <u>k_{SDD}</u> | 0.06 | 0.06 | B |
| <u>k_{pdd}</u> | 0.00 | 0.00 | B |
| <u>k_{fluence}</u> | 0.05 | 0.05 | B |
| <u>k_{profile}</u> | 0.21 | 0.21 | B |
| <u>$N_{D,w}$</u> | 0.75 | 0.75 | B |
| <u>k_Q</u> | 2.10 | 1.40 | B |
| | | | |
| <u>$u(D_{w,SPGC}/D_{w,IC})$</u> | 2.5 | 1.9 | |
| <u>$u(k_Q)$</u> | 1.4 | 1.3 | |

New standard level graphite calorimeter for light-ion beams (cfr Mark Bailey / this workshop)



- Either calibrate ionization chambers or measure k_Q data
- Large enough for scatter build-up
- Light enough to be portable
- Robustness, vacuum operation, core size, perturbation, alignment and beam monitoring considerations

Derivation of $(w_{air})_p$ from calorimeter measurements

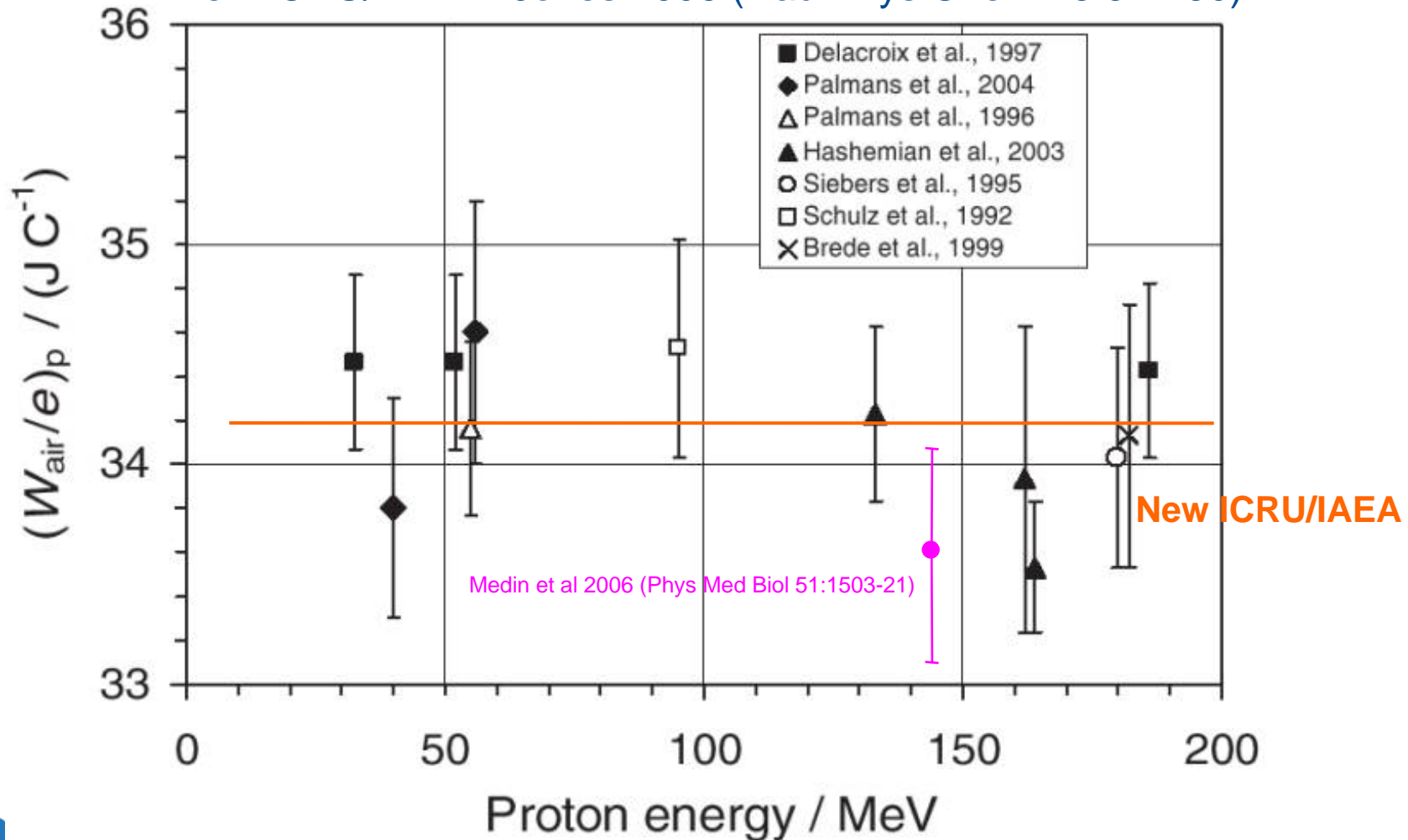
$$k_Q = \frac{N_{D,w,p}}{N_{D,w,c}} = \frac{D_{w,cal,p} / M_p}{N_{D,w,c}} \approx \frac{(w_{air})_p \cdot (s_{w,air})_p \cdot \rho_p}{(W_{air})_c \cdot (s_{w,air})_c \cdot \rho_c}$$

$$(w_{air})_p = \frac{D_{w,cal,p} \cdot (W_{air})_c \cdot (s_{w,air})_c \cdot \rho_c}{M_p \cdot N_{D,w,c} \cdot (s_{w,air})_p \cdot \rho_p}$$

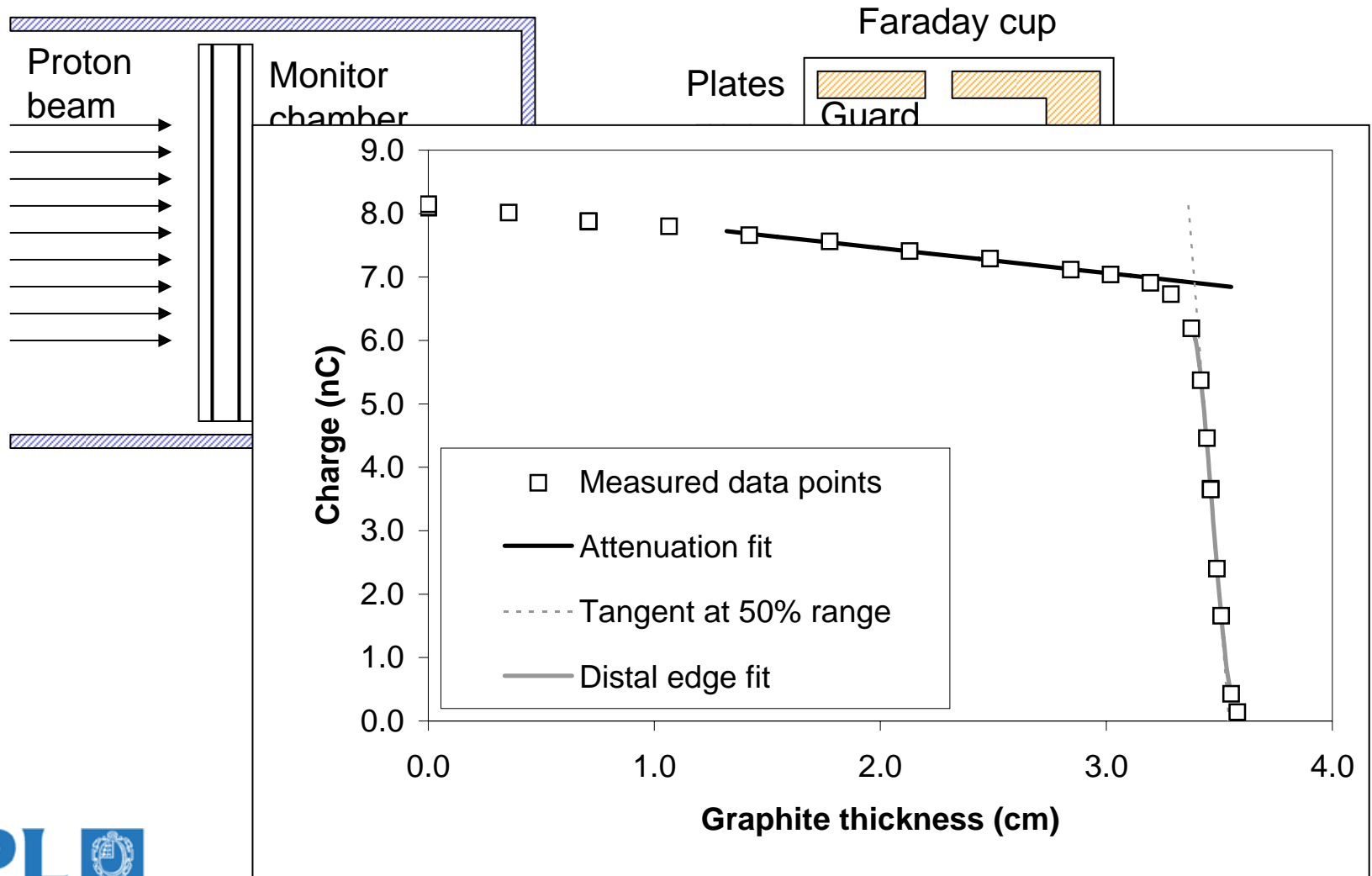
| Calibration beam quality | $(w_{air})_p$ in $J C^{-1}$ | |
|--------------------------|-----------------------------|----------------------|
| | <u>modulated</u> | <u>non-modulated</u> |
| ^{60}Co | 34.1 | 34.9 |
| ^{22}Na | 33.6 | 34.4 |

Importance: new recommendation on proton dosimetry by ICRU/IAEA

New ICRU/IAEA – Jones 2006 (Rad Phys Chem 75:541-50)



Faraday cup measurements for range and attenuation measurements

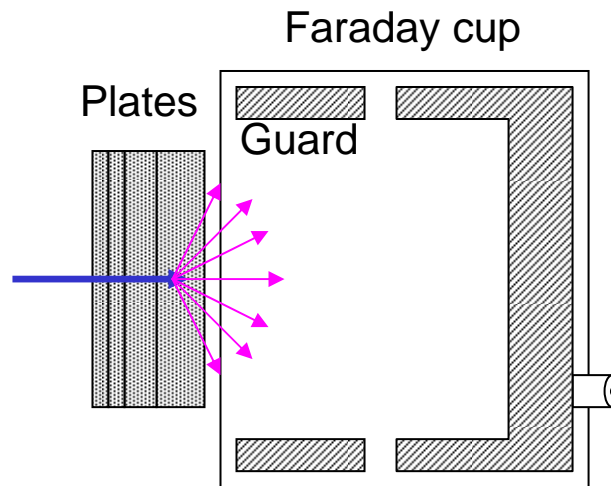


Range results

| Material | Range (g cm ⁻²) <u>measured</u> | Range (g cm ⁻²) ICRU 49 | Difference <u>in g cm⁻²</u> | <u>in mm</u> |
|-------------|--|--|---|--------------|
| Graphite | 3.467 | 3.428 | 0.04 | 0.2 |
| Polystyrene | 3.097 | 3.125 | -0.03 | -0.3 |
| PMMA | 3.143 | 3.150 | -0.01 | -0.1 |
| Aluminium | 3.932 | 4.016 | -0.08 | -0.3 |
| A150 | 3.039 | 3.037 | 0.00 | 0.0 |
| Lead | 6.535 | 6.844 | -0.31 | -0.3 |
| Water | 3.049 | 3.009 | 0.04 | 0.4 |

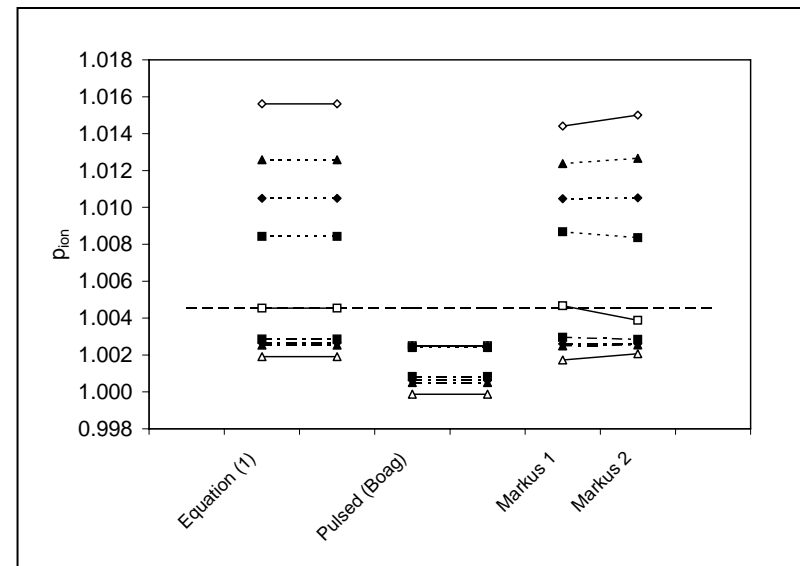
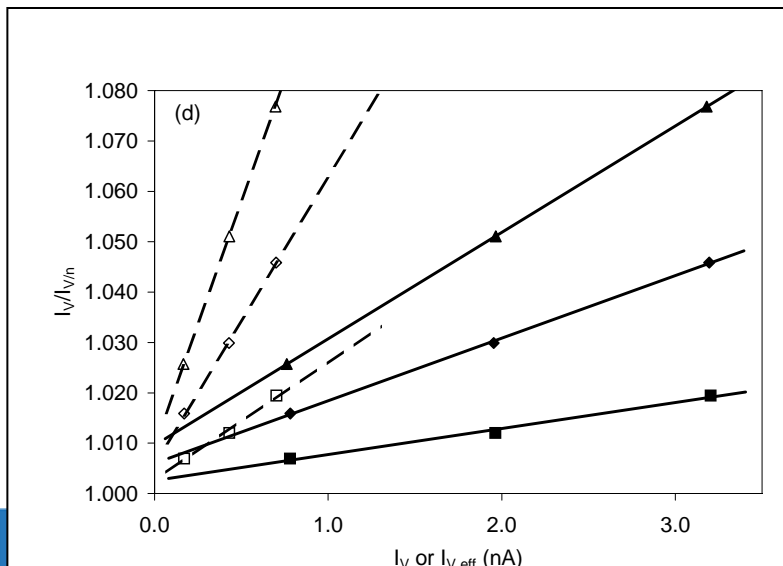
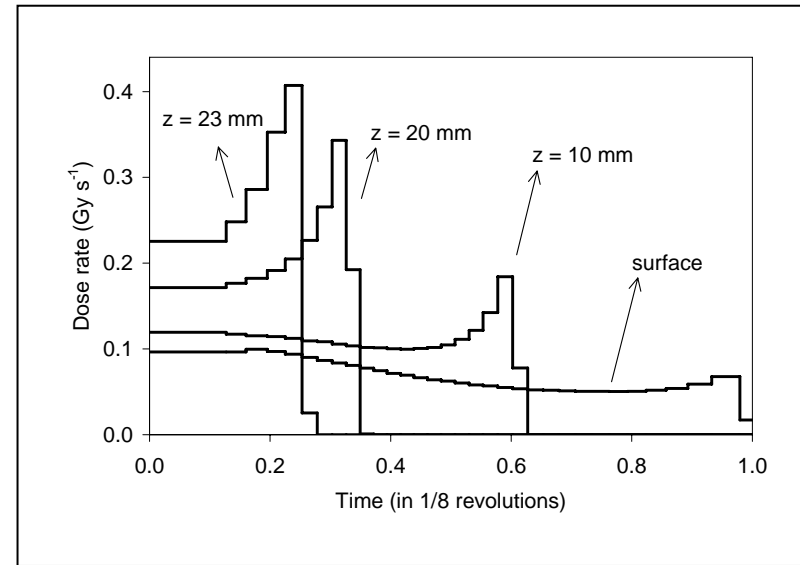
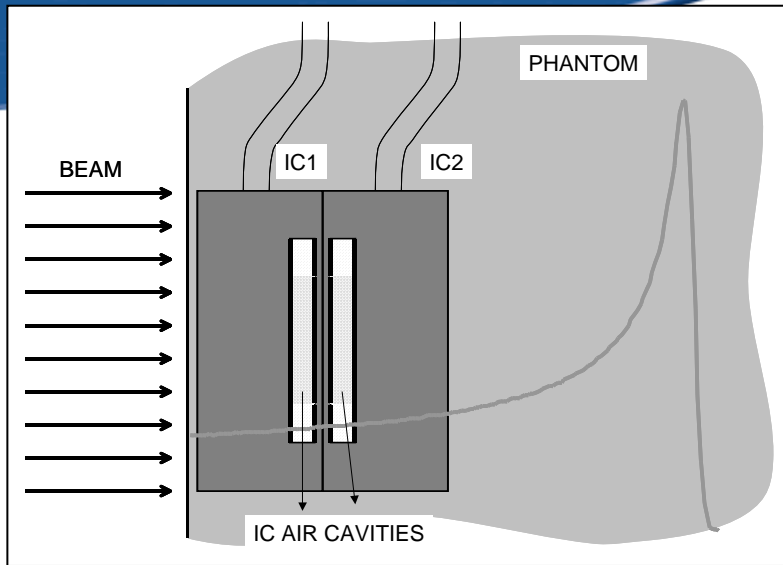
Nuclear attenuation results

- Factor 2 to 3 higher than expected from ICRU 63 tables: not as yet understood.
- Hypothesis: wide angle secondary protons:



Correction factors for ionization chambers: recombination

(Palmans et al 2006, Phys Med Biol 51:903-15)



Perturbation correction factors for ionization chambers

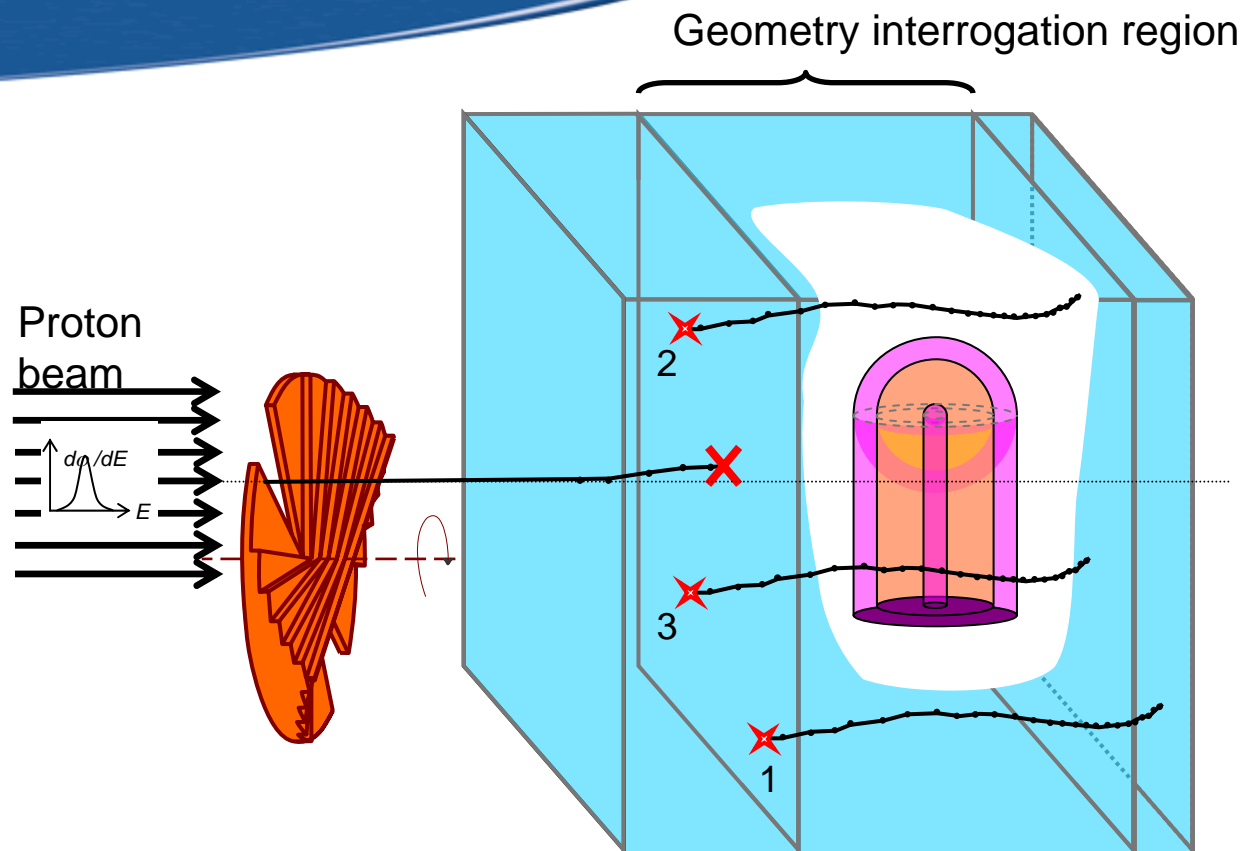
protons



$$D_{water} = D_{air} \cdot \left(\frac{S^{SA}}{\rho} \right)_{air}^{water} \cdot p_{cav} \cdot p_{wall} \cdot p_{cel} \cdot p_{dis}$$

- For high-energy x-rays: typical corrections of level 1% applied since 1970's
- For protons: not applied in any recommendation

ρ_{dis} : Monte Carlo - McPTRAN.CAVITY (Palmans 2006, Phys Med Biol 51:3483-501)



Secondary electrons:

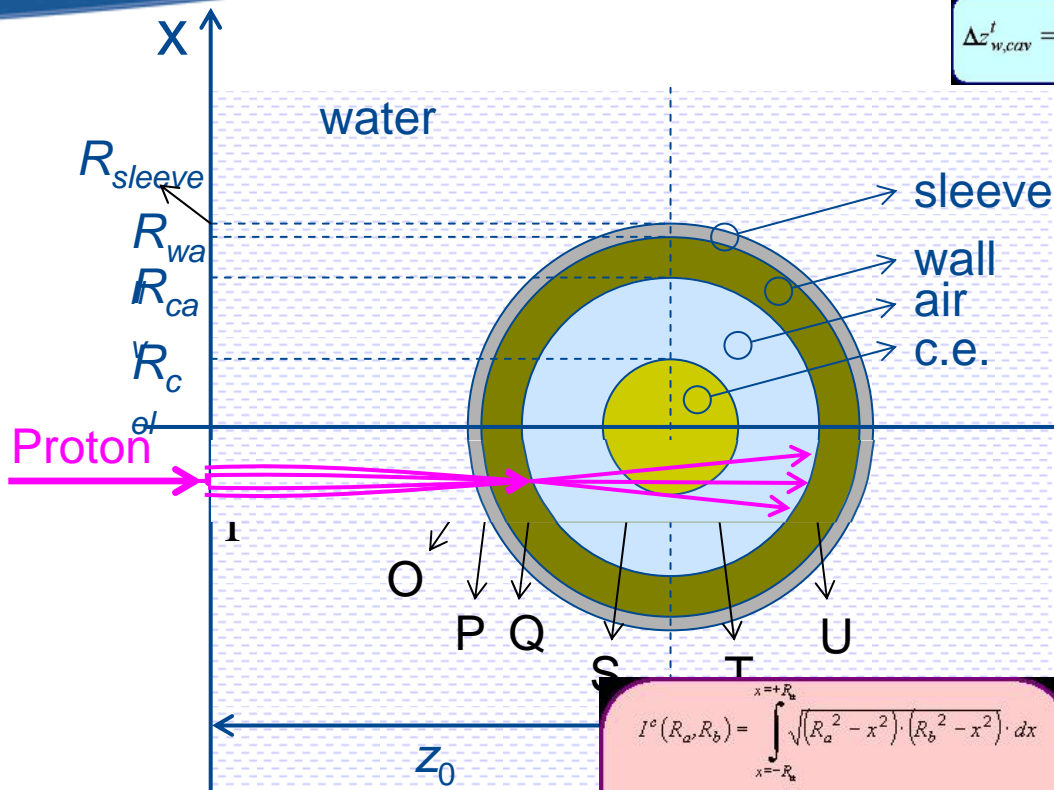
EGSnrc + variance reduction techniques
(Verhaegen&Palmans 2001 *Med. Phys.* 28:2088)

- D in cavities
- ~~~~~
- Histories resumed
Chamber complete
New depth
- ~~~~~
- Variance reduction
Lateral range rejection
History splitting
- ~~~~~
- PDD_{IC} compared
with PDD in
homogeneous
water

p_{dis} : analytical model

Integrating the depth dose curve

(Palmans 2006, Phys Med Biol 51:3483-501)



$$\Delta z_{w,cav}^t = -\frac{K^t(R_{cav})}{J^t(R_{cav})}$$

$$\Delta z_{w,wall}^t = (F_{wall} - 1) \cdot \frac{I^t(R_{cav}, R_{wall}) - K^t(R_{cav})}{J^t(R_{cav})}$$

$$\Delta z_{w,cel}^t = \left[(F_{wall} - 1) \cdot \frac{I^t(R_{cav}, R_{wall})}{J^t(R_{cav})} - F_{wall} \cdot \frac{K^t(R_{cav})}{J^t(R_{cav})} \right] \cdot \frac{\gamma_{cel}^t}{1 - \gamma_{cel}^t} - \left[(F_{wall} - 1) \cdot \frac{I^t(R_{cel}, R_{wall})}{J^t(R_{cav})} - F_{wall} \cdot \frac{I^t(R_{cel}, R_{cav})}{J^t(R_{cav})} \right] \cdot \frac{1}{1 - \gamma_{cel}^t} + F_{cel}^t \cdot \frac{I^t(R_{cel}, R_{cav}) - K^t(R_{cel})}{J^t(R_{cav})} \cdot \frac{1}{1 - \gamma_{cel}^t}$$

$$\Delta z_{w,sleeve}^t = (F_{sleeve} - 1) \cdot \frac{I^t(R_{cav}, R_{sleeve}) - I^t(R_{cav}, R_{wall})}{J^t(R_{cav})} \cdot \frac{1}{1 - \gamma_{cel}^t} - (F_{sleeve} - 1) \cdot \frac{I^t(R_{cel}, R_{sleeve}) - I^t(R_{cel}, R_{wall})}{J^t(R_{cav})} \cdot \frac{1}{1 - \gamma_{cel}^t}$$

$$I^o(R_a, R_b) = \int_{x=-R_a}^{x=+R_a} \sqrt{(R_a^2 - x^2)} \cdot (R_b^2 - x^2) \cdot dx$$

$$J^o(R_a) = \int_{x=-R_a}^{x=+R_a} \sqrt{(R_a^2 - x^2)} \cdot dx = \frac{\pi}{2} \cdot R_a^2$$

$$K^o(R_a) = \int_{x=-R_a}^{x=+R_a} (R_a^2 - x^2) \cdot dx = \frac{4}{3} \cdot R_a^3$$

$$I^s(R_a, R_b) = \int_{r=0}^{r=R_a} \sqrt{(R_a^2 - r^2)} \cdot (R_b^2 - r^2) \cdot r \cdot dr$$

$$= \frac{1}{8} \cdot R_a \cdot R_b \cdot (R_a^2 + R_b^2) + \frac{1}{16} \cdot (R_a^2 - R_b^2)^2 \cdot \ln \left(\frac{R_b - R_a}{R_b + R_a} \right)$$

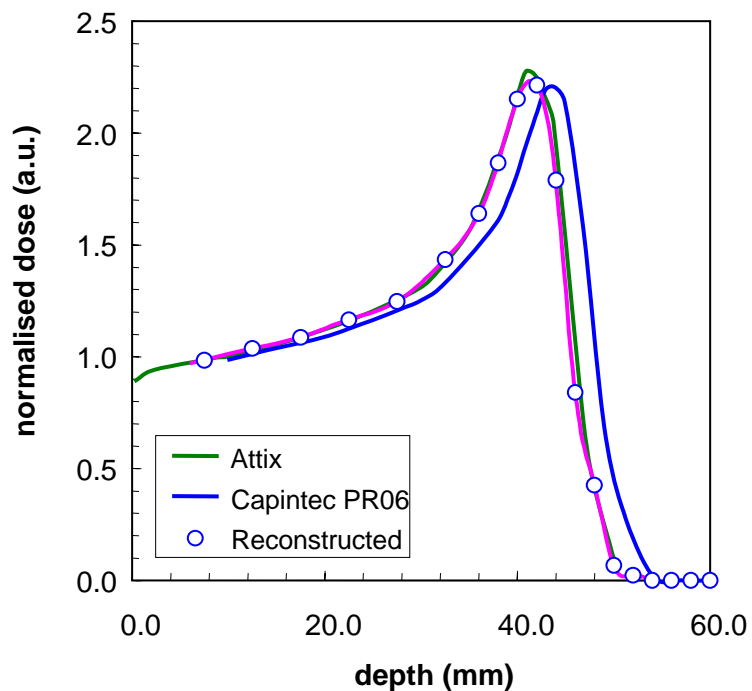
$$J^s(R_a) = \int_{r=0}^{r=R_a} \sqrt{(R_a^2 - r^2)} \cdot r \cdot dr = \frac{1}{3} \cdot R_a^3$$

$$K^s(R_a) = \int_{r=0}^{r=R_a} (R_a^2 - r^2) \cdot r \cdot dr = \frac{1}{4} \cdot R_a^4$$

ρ_{dis} : comparison with experiment PDD's (Palmans 2006, Phys Med Biol 51:3483-501)

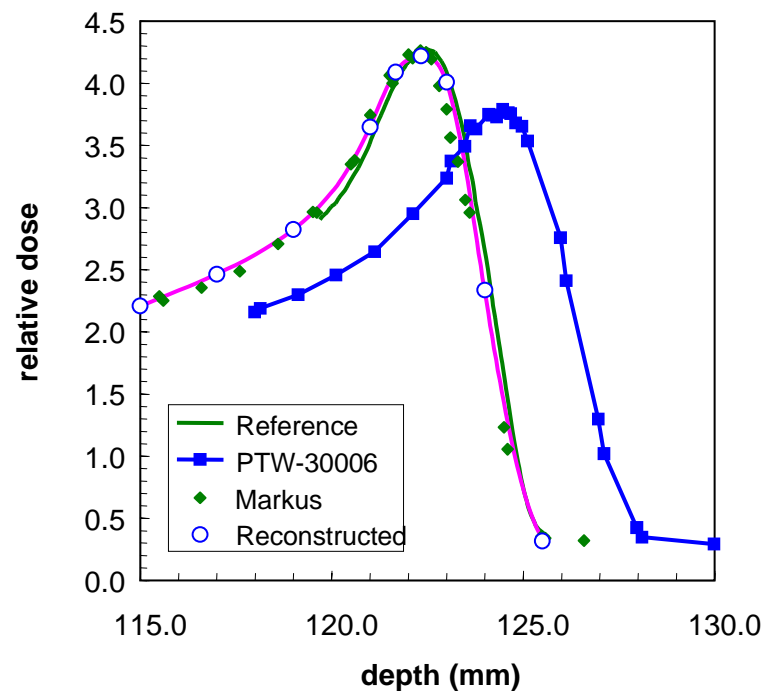
Mobit et al. 2000 *Med. Phys.* 27:2780-2787

78 MeV protons



Jäkel et al. 2000 *Phys. Med. Biol.* 45:599-607

3 GeV ^{12}C

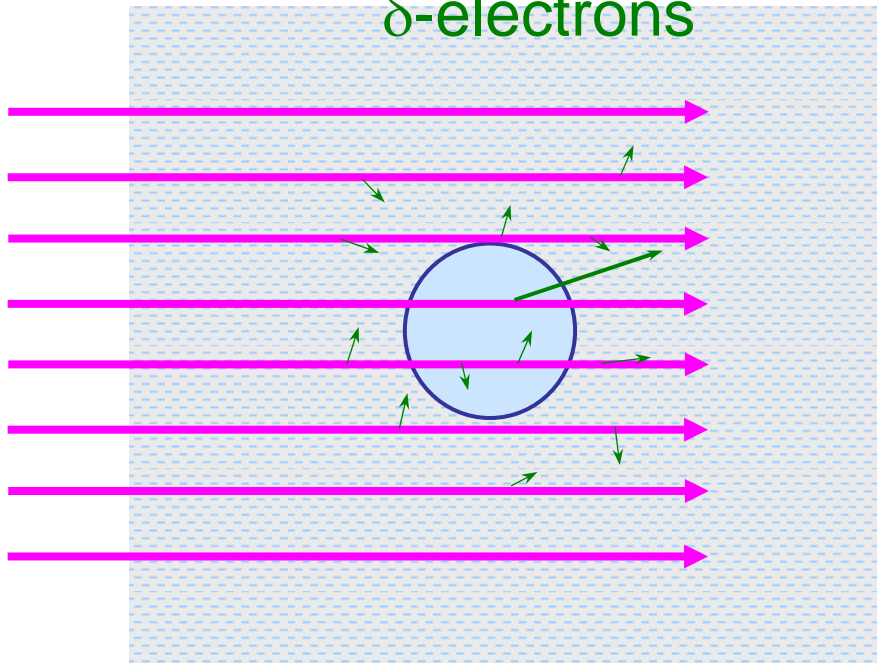


$\rho_{cav,e}$: SA cavity theory

due to secondary electrons

protons

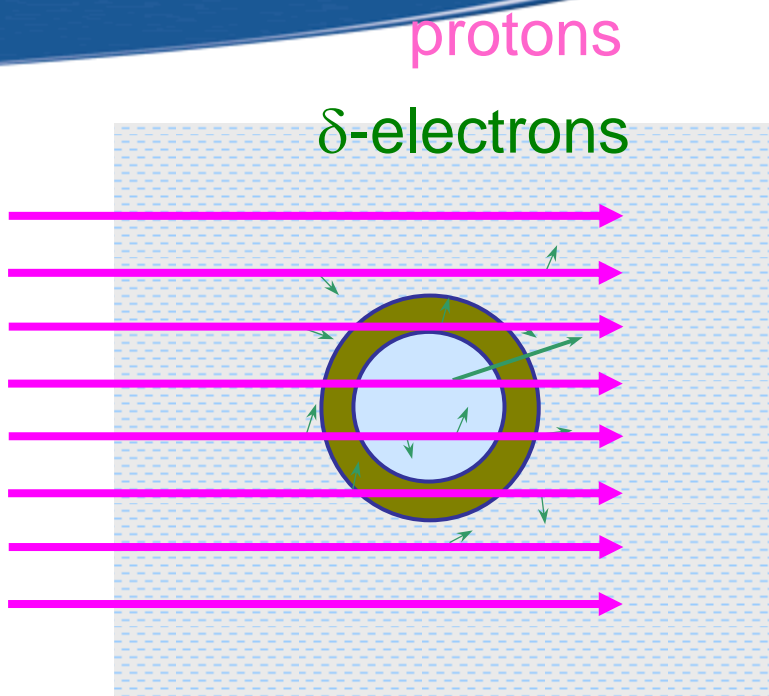
δ -electrons



$$D_{med} = D_{air} \cdot \left(\frac{S^{SA}}{\rho} \right)_{air}^{med}$$
$$= D_{air} \cdot \left(\frac{S}{\rho} \right)_{air}^{med} \cdot \rho_{cav,e}$$

$$\rho_{cav,e} = \left(\frac{S^{SA}}{\rho} \right)_{air}^{med} / \left(\frac{S}{\rho} \right)_{air}^{med}$$

$p_{wall,e}$: SA cavity theory



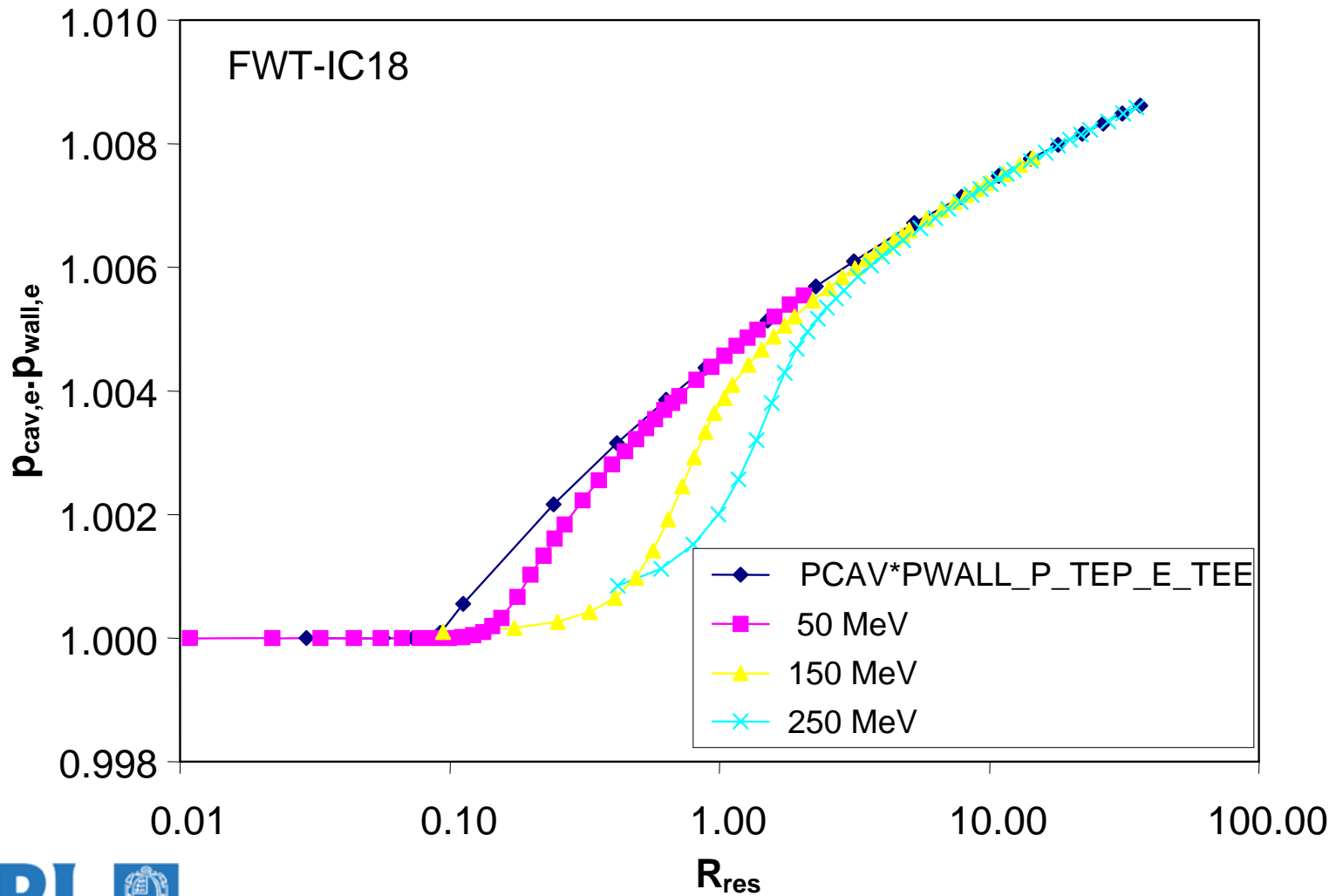
$$D_{med} = D_{air} \cdot \left(\frac{S^{SA}}{\rho} \right)_{air}^{wall} \cdot \left(\frac{S}{\rho} \right)_{wall}^{med}$$

$$= D_{air} \cdot \left(\frac{S^{SA}}{\rho} \right)_{air}^{med} \cdot p_{wall,e}$$

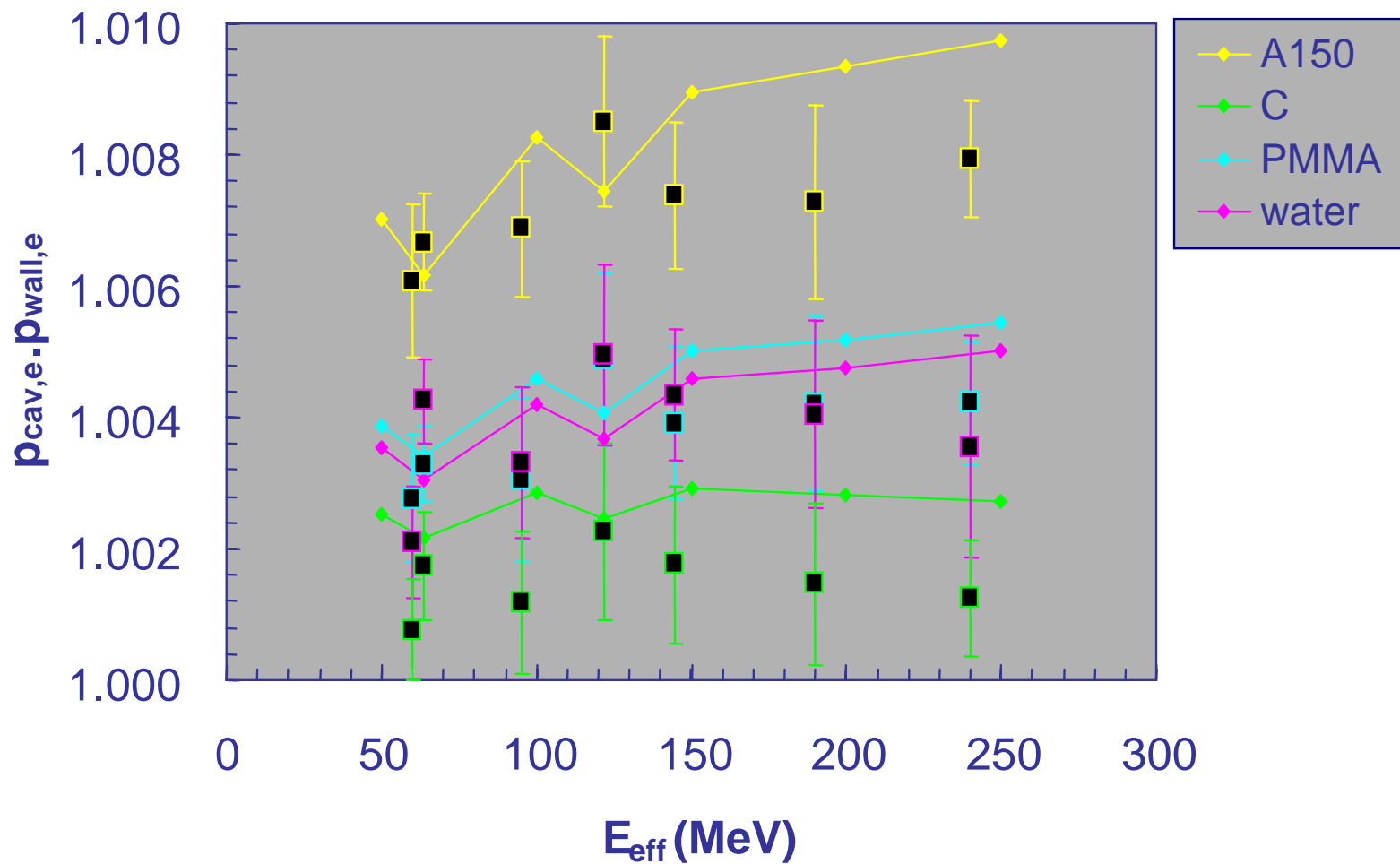
$$p_{wall,e} = \left(\frac{S}{\rho} \right)_{wall}^{med} \cdot \left(\frac{S^{SA}}{\rho} \right)_{air}^{wall} / \left(\frac{S^{SA}}{\rho} \right)_{air}^{med}$$

$\rho_{cav,e}$ & $\rho_{wall,e}$: SA cavity theory for

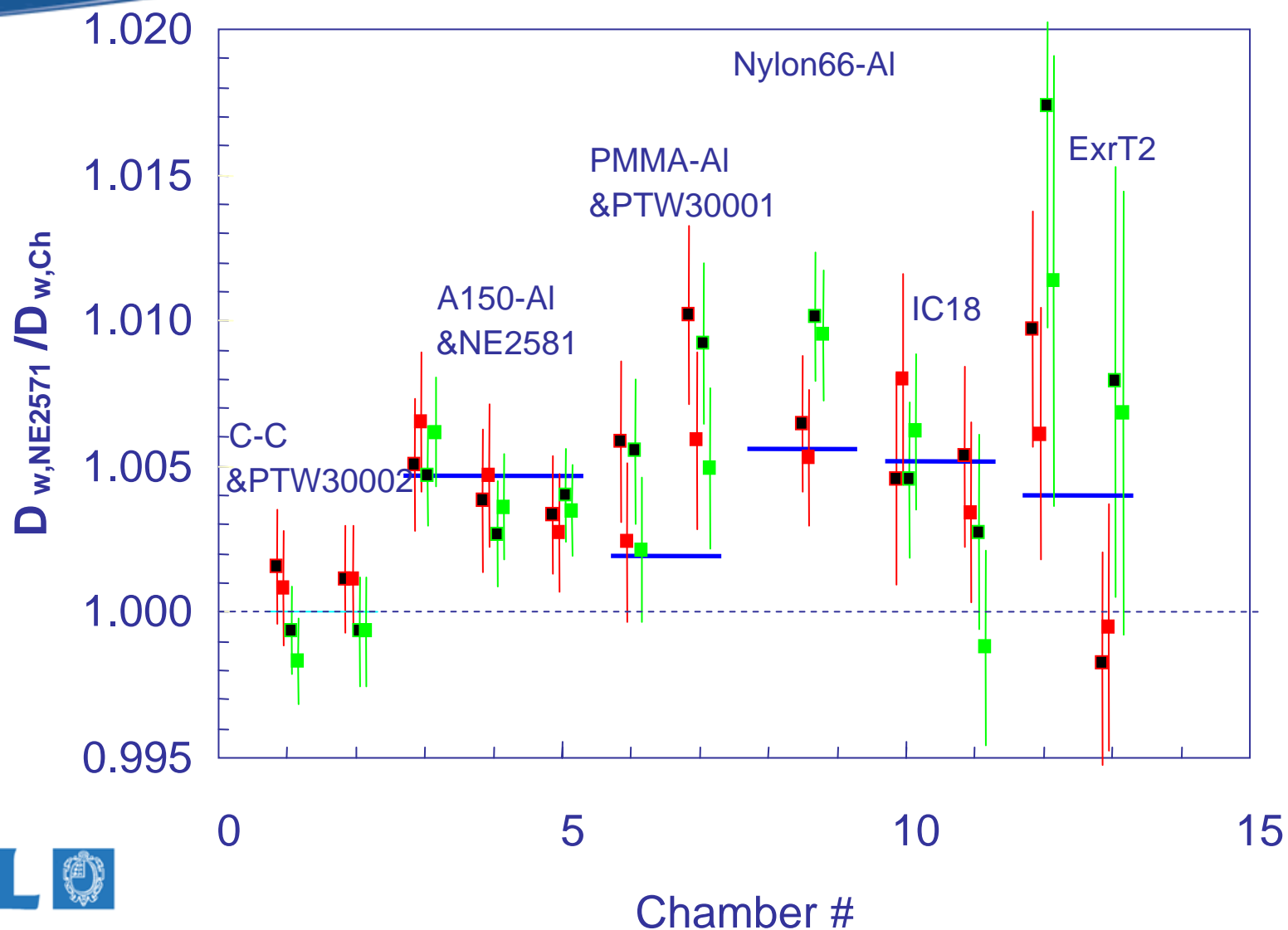
FWT-IC18 type chamber



$\rho_{cav,e}$ & $\rho_{wall,e}$: Monte Carlo versus SA cavity theory (spher $r = 0.25\text{cm}$, $\Delta = 13.2$ keV)



$\rho_{cav,e}$ & $\rho_{wall,e}$: comparison with experiment



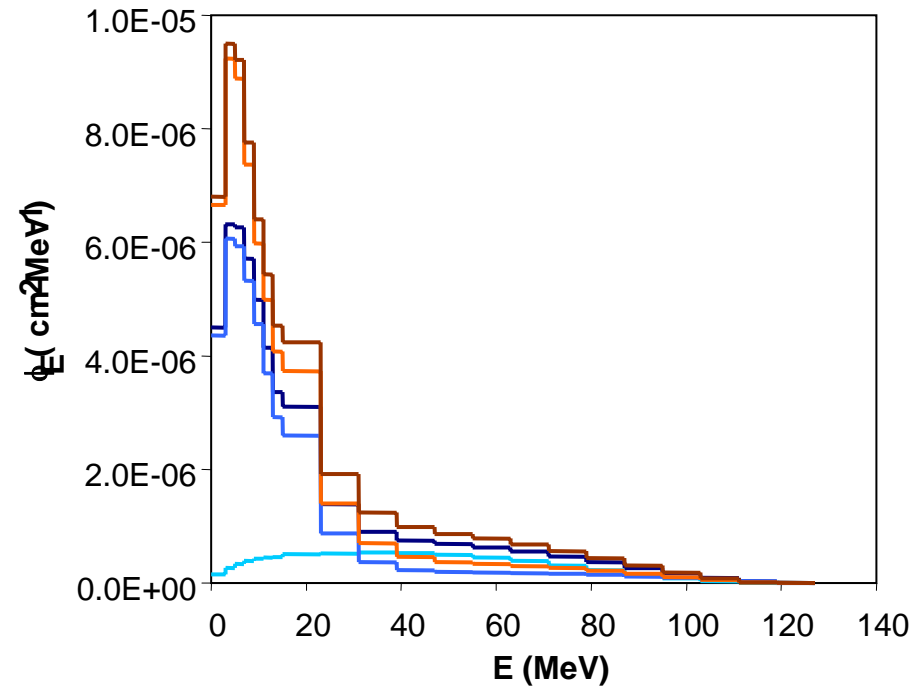
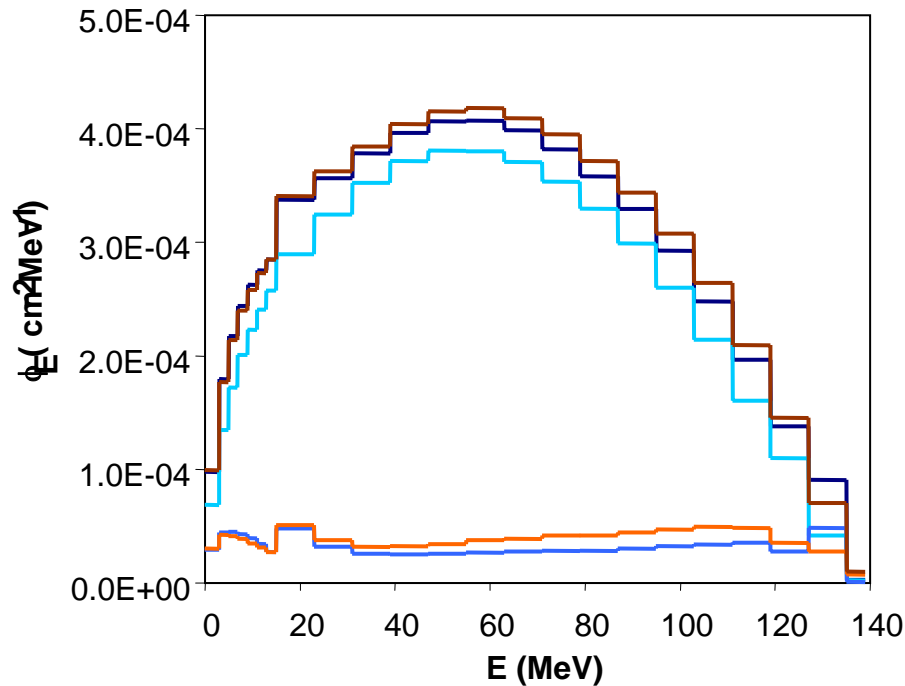
$\rho_{\text{wall},n}$: (simplistic) analytical model for slowing down spectra secondary p & α (NE2571, 150 MeVp)

due to secondaries from nonelastic nuclear interactions

p:

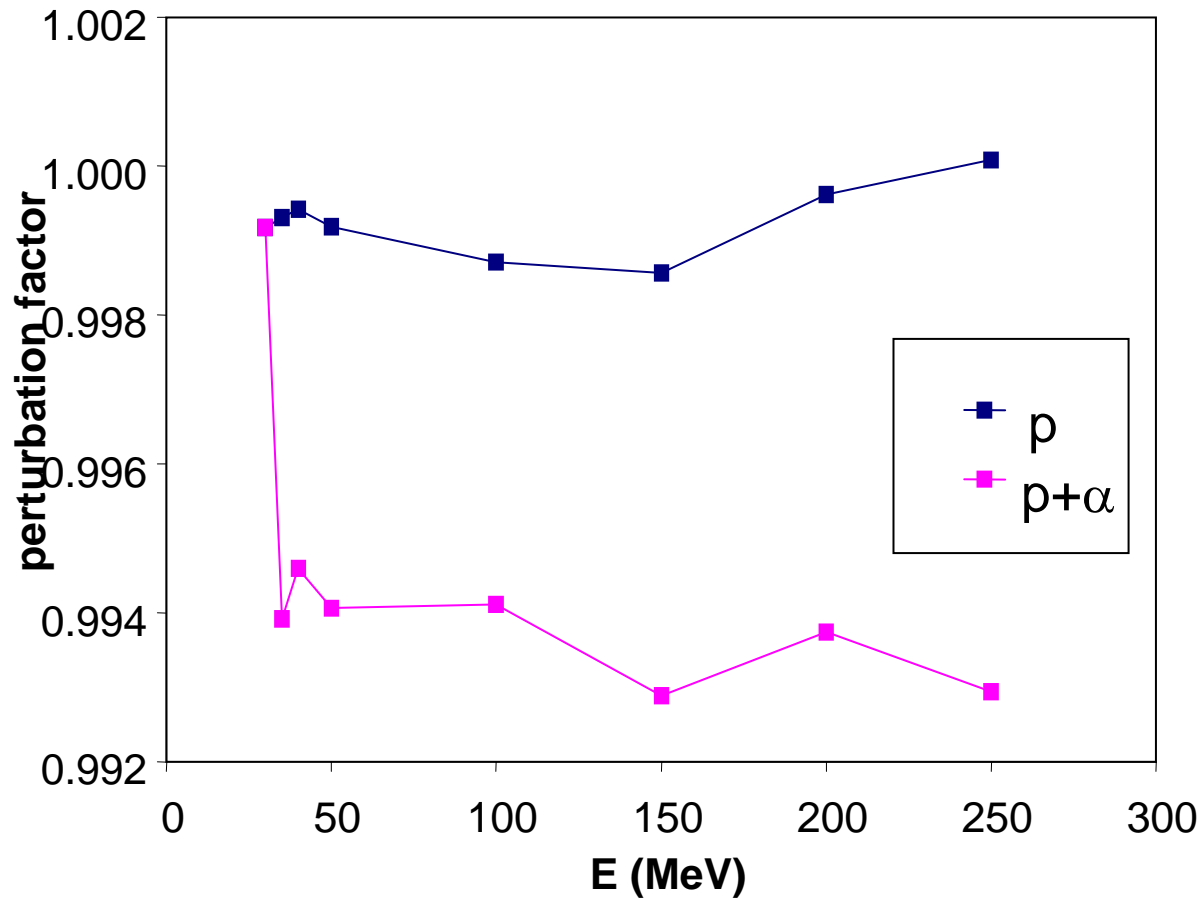
water bulk

α :



“water” wall

graphite wall



- BUT:
- ICRU 63 data ($u_C \sim 30-40\%$)
- Crude model
- → MC study needed

- Graphite calorimetry

Many operation characteristics, perturbation factors and heat transfer phenomena are similar as for photons

Primary standard level calorimeter is being built

Conversion to dose to water is a serious issue

- Interaction/basic data:

Substantial contribution to $(w_{\text{air}})_p$ value

Range and attenuation measurements

- Ionization chambers

Corrections for recombination, gradients and secondary electrons

Further work: non-elastic nuclear interactions

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